

Constants:

$$\begin{aligned}
g &\approx 9.81 \text{ m/s}^2 \\
N_A &= 6.022 \times 10^{23} \text{ things/mol} \\
k_e &\equiv 1/4\pi\epsilon_0 = 8.98755 \times 10^9 \text{ N} \cdot \text{m}^2 \cdot \text{C}^{-2} \\
\epsilon_0 &= 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2 \\
\mu_0 &\equiv 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A} \\
e &= 1.60218 \times 10^{-19} \text{ C} \\
h &= 6.6261 \times 10^{-34} \text{ J} \cdot \text{s} = 4.1357 \times 10^{-15} \text{ eV} \cdot \text{s} \\
\hbar &= \frac{h}{2\pi} \\
k_B &= 1.38065 \times 10^{-23} \text{ J} \cdot \text{K}^{-1} = 8.6173 \times 10^{-5} \text{ eV} \cdot \text{K}^{-1} \\
c &= \frac{1}{\sqrt{\mu_0\epsilon_0}} = 2.99792 \times 10^8 \text{ m/s} \\
hc &= 1240 \text{ eV} \cdot \text{nm} \\
m_e &= 9.10938 \times 10^{-31} \text{ kg} \quad m_e c^2 = 510.998 \text{ keV} \\
m_p &= 1.67262 \times 10^{-27} \text{ kg} \quad m_p c^2 = 938.272 \text{ MeV}
\end{aligned}$$

Quadratic formula:

$$0 = ax^2 + bx^2 + c \implies x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Basic Equations:

$$\begin{aligned}
\vec{\mathbf{E}} &= \sigma/\epsilon_0 \text{ capacitor} \\
C &= \epsilon_0 A/d \\
\vec{\mathbf{F}}_{\text{net}} &= m\vec{\mathbf{a}} \text{ Newton's Second Law} \\
\vec{\mathbf{F}}_{\text{centr}} &= -\frac{mv^2}{r} \hat{\mathbf{r}} \text{ Centripetal} \\
K_{\text{classical}} &= \frac{1}{2}mv^2 \\
0 &= ax^2 + bx^2 + c \implies x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}
\end{aligned}$$

E & M

$$\begin{aligned}
\vec{\mathbf{F}}_{12} &= k_e \frac{q_1 q_2}{r_{12}^2} \hat{\mathbf{r}}_{12} = q_2 \vec{\mathbf{E}}_1 \quad \vec{\mathbf{r}}_{12} = \vec{\mathbf{r}}_1 - \vec{\mathbf{r}}_2 \\
\vec{\mathbf{E}}_1 &= \vec{\mathbf{F}}_{12}/q_2 = k_e \frac{q_1}{r_{12}^2} \hat{\mathbf{r}}_{12} \\
\vec{\mathbf{F}}_B &= q\vec{\mathbf{v}} \times \vec{\mathbf{B}} \\
U_{12} &= k_e \frac{q_1 q_2}{r_{12}} \text{ potential E, 2 charges}
\end{aligned}$$

Oscillators & waves

$$\begin{aligned}
E &= \frac{1}{2}kA^2 = \frac{1}{2}\omega^2 mA^2 = 2\pi^2 m f^2 A^2 \\
\omega &= 2\pi f = \sqrt{k/m} \\
c &= \lambda f
\end{aligned}$$

Approximations, $x \ll 1$

$$\begin{aligned}
(1+x)^n &\approx 1 + nx + \frac{1}{2}n(n+1)x^2 \quad e^x \approx 1 + x + \frac{1}{2}x^2 \\
\sin x &\approx x - \frac{1}{6}x^3 \quad \cos x \approx 1 - \frac{1}{2}x^2
\end{aligned}$$

Radiation

$$P_{\text{rad}} = \frac{q^2 a^2}{6\pi\epsilon_0 c^3} \quad \text{total emitted power, } E \text{ and } B \text{ fields}$$

Relativity

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$\Delta t'_{\text{moving}} = \gamma \Delta t_{\text{stationary}} = \gamma \Delta t_p$$

$$L'_{\text{moving}} = \frac{L_{\text{stationary}}}{\gamma} = \frac{L_p}{\gamma}$$

$$x' = \gamma(x - vt) \quad x = \gamma(x' + vt')$$

$$t' = \gamma\left(t - \frac{vx}{c^2}\right) \quad t = \gamma\left(t' + \frac{vx'}{c^2}\right)$$

$$v_{\text{obj}} = \frac{v + v'_{\text{obj}}}{1 + \frac{vv'_{\text{obj}}}{c^2}} \quad v'_{\text{obj}} = \frac{v_{\text{obj}} - v}{1 - \frac{vv_{\text{obj}}}{c^2}}$$

$$\text{KE} = (\gamma - 1)mc^2 = \sqrt{m^2 c^4 + c^2 p^2} - mc^2$$

$$E_{\text{rest}} = mc^2$$

$$p = \gamma mv$$

$$E^2 = p^2 c^2 + m^2 c^4 = (\gamma mc^2)^2$$

Calculus of possible utility:

$$\int \frac{1}{x} dx = \ln x + c$$

$$\int u dv = uv - \int v du$$

Vectors:

$$|\vec{\mathbf{F}}| = \sqrt{F_x^2 + F_y^2} \quad \text{magn} \quad \theta = \tan^{-1} \left[\frac{F_y}{F_x} \right] \quad \text{dir}$$