

Constants:

$$\begin{aligned}
 k_e &\equiv 1/4\pi\epsilon_o = 8.98755 \times 10^9 \text{ N} \cdot \text{m}^2 \cdot \text{C}^{-2} \\
 \epsilon_o &= 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2 \\
 \mu_o &\equiv 4\pi \times 10^{-7} \text{ T} \cdot \text{m}/\text{A} \\
 c^2 &= 1/\mu_o\epsilon_o \\
 e &= 1.60218 \times 10^{-19} \text{ C} \\
 m_{e^-} &= 9.10938 \times 10^{-31} \text{ kg} \\
 m_{p^+} &= 1.67262 \times 10^{-27} \text{ kg} \\
 1 \text{ u} &= 931.494 \text{ MeV}/c^2 \\
 g &= 9.81 \text{ m}/\text{s}^2
 \end{aligned}$$

Basic Equations:

$$\begin{aligned}
 0 &= ax^2 + bx^2 + c \implies x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\
 \vec{F}_{\text{centr}} &= -\frac{mv^2}{r} \hat{r} \text{ Centripetal}
 \end{aligned}$$

Electric Force & Field:

$$\begin{aligned}
 \vec{F}_{12} &= k_e \frac{q_1 q_2}{r^2} \hat{r} = q_2 \vec{E}_1 \\
 \vec{E}_1 &= \vec{F}_{12}/q_2 = k_e \frac{q_1}{r^2} \hat{r} \\
 \vec{E} &= k_e \sum_i \frac{q_i}{r_i^2} \hat{r}_i \rightarrow k_e \int \frac{dq}{r^2} \hat{r} = k_e \int \frac{\rho \hat{r}}{r^2} dV_{ol}
 \end{aligned}$$

Electric Potential (static case!):

$$\begin{aligned}
 \Delta V &= V_B - V_A = \frac{\Delta U}{q} = -\int_A^B \vec{E} \cdot d\vec{l} \\
 V_{\text{point}} &= k_e \frac{q}{r} \\
 V &= k_e \int \frac{dq}{r} \text{ continuous} \\
 E_x &= -\frac{dV}{dx} \rightarrow \vec{E} = -\nabla V \\
 Q &= C\Delta V \text{ capacitor}
 \end{aligned}$$

Current & Resistance:

$$\begin{aligned}
 I &= \int_S \vec{J} \cdot d\vec{A} \xrightarrow{\text{uniform J}} I = \frac{dQ}{dt} = nqAv_d \\
 J &= \frac{I}{A} = nqv_d \text{ uniform J} \\
 \int_S \vec{J} \cdot d\vec{A} &= -\frac{d}{dt} \int_V \rho dV_{ol} \\
 R &= \frac{\rho l}{A} \quad \rho = 1/\sigma \\
 \mathcal{P} &= U \cdot \Delta t = I\Delta V \text{ power} \\
 R_{\text{eq}} &= R_1 + R_2 + \dots \text{ series} \\
 1/R_{\text{eq}} &= 1/R_1 + 1/R_2 + \dots \text{ parallel} \\
 \sum I_{\text{in}} &= \sum I_{\text{out}} \text{ junction} \\
 \sum_{\text{closed path}} \Delta V &= 0 \text{ loop}
 \end{aligned}$$

Magnetism:

$$\begin{aligned}
 \vec{F}_B &= q\vec{v} \times \vec{B} \\
 d\vec{F}_B &= Id\vec{l} \times \vec{B} \text{ I-carrying wire} \\
 d\vec{B} &= \frac{\mu_o}{4\pi} \frac{Id\vec{l} \times \hat{r}}{r^2} \text{ wire} \\
 B &= \frac{\mu_o NI}{l} = \mu_o nI \text{ solenoid} \\
 \frac{F_B}{l} &= \frac{\mu_o I_1 I_2}{2\pi d} \text{ 2 wires} \\
 \Phi_B &= \oint \vec{B} \cdot d\vec{A} \\
 \vec{\tau} &= \vec{\mu} \times \vec{B} \text{ with } \vec{\mu} = I\vec{A} \text{ 1 loop} \\
 U &= -\vec{\mu} \times \vec{B}
 \end{aligned}$$

Induction & Maxwell

$$\begin{aligned}
 \Delta V &= \oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt} \\
 \Delta V &= Blv \text{ motional} \\
 \Phi_E &= \oint \vec{E} \cdot d\vec{A} = 4\pi k_e q_{\text{encl}} = \frac{q_{\text{encl}}}{\epsilon_o} \\
 \oint \vec{B} \cdot d\vec{A} &= 0 \\
 \oint \vec{B} \cdot d\vec{l} &= \mu_o I + \frac{1}{c^2} \frac{d\Phi_E}{dt}
 \end{aligned}$$

Vectors:

$$\begin{aligned}
 |\vec{F}| &= \sqrt{F_x^2 + F_y^2} \text{ magnitude} \\
 \theta &= \tan^{-1} \left[\frac{F_y}{F_x} \right] \text{ direction} \\
 \hat{r} &= \vec{r}/|\vec{r}| \\
 d\vec{l} &= dx \hat{x} + dy \hat{y} + dz \hat{z} \\
 \text{let } \vec{a} &= a_x \hat{x} + a_y \hat{y} + a_z \hat{z} \text{ and } \vec{b} = b_x \hat{x} + b_y \hat{y} + b_z \hat{z} \\
 \vec{a} \cdot \vec{b} &= a_x b_x + a_y b_y + a_z b_z = \sum_{i=1}^n a_i b_i = |\vec{a}| |\vec{b}| \cos \theta \\
 |\vec{a} \times \vec{b}| &= |\vec{a}| |\vec{b}| \sin \theta \\
 \vec{a} \times \vec{b} &= \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix} = (a_y b_z - a_z b_y) \hat{x} + (a_z b_x - a_x b_z) \hat{y} + (a_x b_y - a_y b_x) \hat{z}
 \end{aligned}$$

Derived unit	Symbol	equivalent to
newton	N	kg·m/s ²
joule	J	kg·m ² /s ² = N·m
watt	W	J/s = m ² ·kg/s ³
coulomb	C	A·s
V	W/A = m ² ·kg/·s ³ ·A	
farad	F	C/V = A ² ·s ⁴ /m ² ·kg
ohm	Ω	V/A = m ² ·kg/s ³ ·A ²
tesla	T	Wb/m ² = kg/s ² ·A
electron volt	eV	1.6 × 10 ⁻¹⁹ J
-	1 T · m/A	1 N/A ²
-	1 T · m ²	1 V · s
-	1 N/C	1 V/m

Right-hand rule #1

1. Point the fingers of your right hand along the direction of \vec{v} .
2. Point your thumb in the direction of \vec{B} .
3. The magnetic force on a + charge points out from the back of your hand.

Right-hand rule #2:

Point your right thumb along the wire in the direction of the current. Your fingers curl around the direction of the magnetic field, which circulates around the wire.