

Name \_\_\_\_\_

## PH 125 Quiz 5: Its not Work if you do it right

$$W = \int_{r_i}^{r_f} \vec{F} \cdot d\vec{r} = \int_{x_i}^{x_f} F_x \cdot dx \quad \Sigma W = K_f - K_i = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

1. The magnitude of the force on a spring as a function of its displacement from equilibrium ( $x = 0$ ) can be written  $F = -kx$ , where  $k$  is the "force constant" of the spring. What is the amount of work done in stretching the spring from  $x = 0$  to  $x = x_f$ ?

We need only integrate the force through the displacement. If the displacement is purely along the  $x$  axis from  $x = 0$  to  $x_f$ , we can write an incremental displacement as  $d\vec{x} = dx \hat{i}$ , whereas the force can be written  $\vec{F} = -kx \hat{i}$ , acting in the opposite direction as the displacement.

$$W = \int_0^{x_f} \vec{F} \cdot d\vec{x} = \int_0^{x_f} (-kx \hat{i}) \cdot (dx \hat{i}) = \int_0^{x_f} -kx dx = \left[ -\frac{1}{2}kx^2 \right]_0^{x_f} = -\frac{1}{2}kx_f^2$$

2. What is the work done when a 3 kg object free-falls 1 m straight down, relative to the earth's surface? You can neglect air resistance, and let  $g = 10 \text{ m/s}^2$ .

The work done by gravity is just the net vertical displacement times the object's weight:

$$W_g = mg\Delta y = (3 \text{ kg}) (10 \text{ m/s}^2) (1 \text{ m}) = 30 \text{ J}$$

3. If you did *not* ignore air resistance in question 2, which of the following would be true?

- The work done would be more, work is done against air resistance and gravity.
- The work done would be less, air resistance is countering work by gravity.
- The work done would be the same, the force of air resistance does no work.
- Cannot be determined without knowing the precise nature of the force of air resistance.

The work done by *gravity* is exactly the same, since the force of gravity itself does not change and neither does the total distance fallen.

A more formal answer would be that air resistance doesn't do any work, since it is not a force acting through a point of displacement, but a force acting over the whole object itself. We'll get in to that.